Vector-borne disease outbreak control via instant vector releases

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> Congrès Nationale d'Analyse Numérique Evian-les-Bains

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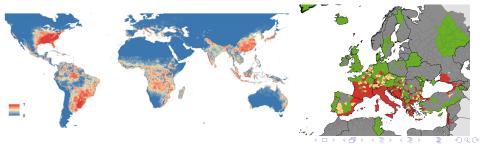
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- No efficient vaccine, nor antiviral drugs.
- Expansion of vector's habitat (trade, global warming, reduction of predator populations ...)

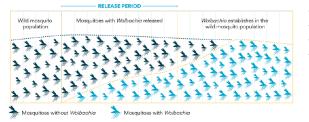


How to fight it? Two methods

• Wolbachia method

- Reduction of the vector capacity.
- Cytoplasmic incompatibility.

- Wolbachia vertical transmission.
- Population replacement.



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Source: http://www.eliminatedengue.com/our-research/Wolbachia

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Wolbachia establishes in the wild mosquito population

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• Sterile insect technique

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- Population suppression.

- Recurrent intervention

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$$S'_{H} = b_{H}H - \frac{\beta_{M}}{H}I_{M}S_{H} - b_{H}S_{H}$$
$$E'_{H} = \frac{\beta_{M}}{H}I_{M}S_{H} - \gamma_{H}E_{H} - b_{H}E_{H}$$
$$I'_{H} = \gamma_{H}E_{H} - \sigma_{H}I_{H} - b_{H}I_{H}$$

$$M' = b_M M \left(1 - \frac{M}{K} \right) - d_M M$$

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Impulsive control: $u(t) = \sum_{i=1}^{n} c_i \delta(t - t_i)$ Constraint: $\sum_{i=1}^{n} c_i = C$

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Goal: Minimise J(u) during an outbreak

$$J(u) := \int_0^T I_H(t) dt$$

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Numerics

We compute $\frac{\delta J(u)}{\delta t_i}$ and $\frac{\delta J(u)}{\delta c_i}$ and we implement a numerical algorithm.

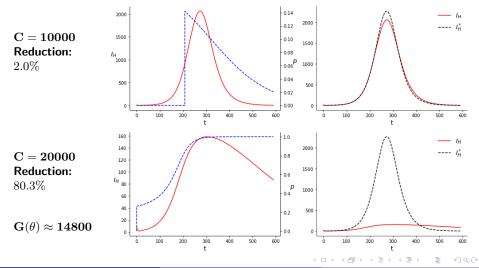
• For the t_i : Gradient descent

• For the c_i : Uzawa algorithm to deal with the constraint $\sum_{i=1}^{n} c_i = C$.

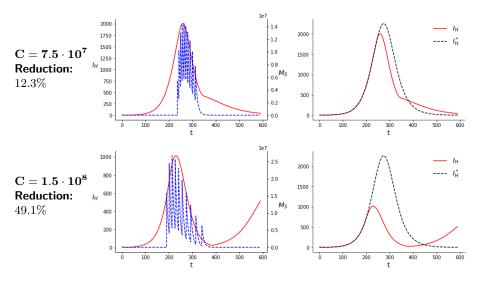
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Results: Wolbachia

- $C < G(\theta)$: release before the outbreak reaches its peak.
- $C > G(\theta)$: Release at t = 0.



Results SIT: 10 releases

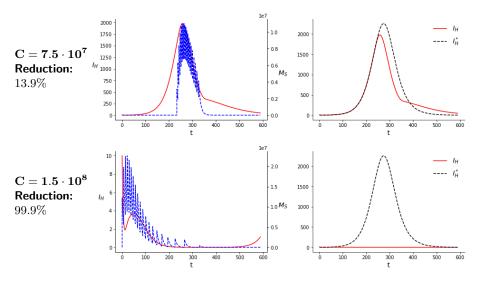


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Results SIT: 20 releases



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 - Optimal strategy: One single release
 - If we have enough mosquitoes to trigger a population replacement: release as soon as possible.
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 - Strategy and results depend highly on the number of jumps at first.
 - After $\sim 20~{\rm jumps}$ almost no improvement.
 - With few mosquitoes: spaced releases around the peak.
 - With a lot of mosquitoes: spaced releases from the begginning.

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Thank you for your attention

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